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Z-dependent spectral measurements of SASE FEL radiation at APS[☆]

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Abstract

We report on the first measurements of the z -dependence of the spectrum of self-amplified spontaneous emission free-electron laser (SASE FEL) radiation. The measurements are performed under different FEL conditions in the wavelength range from 265 to 530 nm. Spectral measurements of the radiation at FEL saturation are included. The z -dependence of the radiation spectrum is compared with theory and simulations. © 2002 Published by Elsevier Science B.V.

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1. Introduction

The low-energy undulator test line (LEUTL) at the Advanced Photon Source (APS) is designed to conduct experiments on the self-amplified spontaneous emission free-electron laser (SASE FEL) process in the visible and ultraviolet wavelengths. It was built as an extension of the existing APS linac and includes a photocathode RF gun, a linear accelerator with a bunch compressor, an electron beam transport line, and an undulator system.

The photocathode RF gun generates high-current low-emittance electron bunches at 6 Hz.

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The linear accelerator can accelerate the electron beam up to a maximum of 650 MeV, but for present SASE experiments the energy ranges from 217 to 300 MeV. The undulator system consists of nine identical 2.4 m long undulators separated from each other by a 38 cm long drift space containing visible light diagnostics (VLD) station, and quadrupole and corrector magnets. The undulator period is 3.3 cm, the peak field is 1 T, and the undulator parameter K is 3.1. A detailed description of the LEUTL and its various component systems can be found in Refs. [1–4].

Last year outstanding results were obtained at the LEUTL. The gain from the first undulator to the saturation point of the order of 10^6 was measured, and the saturation of the SASE FEL process was achieved in visible and ultraviolet [5].

This paper presents spectral data of the SASE light gathered during that time, their analysis, and

1 comparison with theory and simulation results.
 2 The paper begins with the description of a high-
 3 resolution spectrometer. Then it describes the
 4 spectrum measurements and presents the first z -
 5 dependent spectral measurements of the SASE
 6 light. Simulation results are also presented to
 7 compare with the measurements. Finally, the
 8 dependence of the radiated wavelength on the
 9 vertical angle is discussed, and an example of the
 10 second harmonic spectrum is demonstrated.

13 2. Spectrometer description

15 All spectral measurements reported in this paper
 16 have been done with a high-resolution spectrom-
 17 eter located at the downstream end of the
 18 undulator line in the end-station room. A mirror
 19 at each diagnostic station can direct the SASE
 20 light towards the spectrometer through a hole in
 21 the shielding wall, thus allowing one to measure
 22 spectral characteristics of the SASE light at
 23 different longitudinal locations along the undula-
 24 tor line.

49 A schematic of the spectrometer is shown in Fig
 50 1. It utilizes a Paschen–Runge mount. This design
 51 was chosen because of its great flexibility: it
 52 provides independence on the angle of the incom-
 53 ing light, it can be tuned for wide range of
 54 wavelengths, and it is easy to modify. The
 55 spectrometer consists of three main elements all
 56 located on the Rowland circle: a vertical entrance
 57 slit, a spherical grating, and a CCD camera. The
 58 light coming from the undulator hall is focused
 59 on the entrance slit with a concave mirror. All
 60 optical elements are reflective with metal coatings.
 61 This allows the system to work over a wide range of
 62 wavelengths. The CCD camera can measure the
 63 radiation of each electron bunch separately. To
 64 reduce the dark current and to improve the signal-
 65 to-noise ratio, the CCD camera is cooled.

66 The spectrometer was calibrated with hollow
 67 cathode discharge lamps, and the designed resolu-
 68 tion was checked on different wavelengths. The
 69 main parameters of the spectrometer are presented
 70 in Table 1.

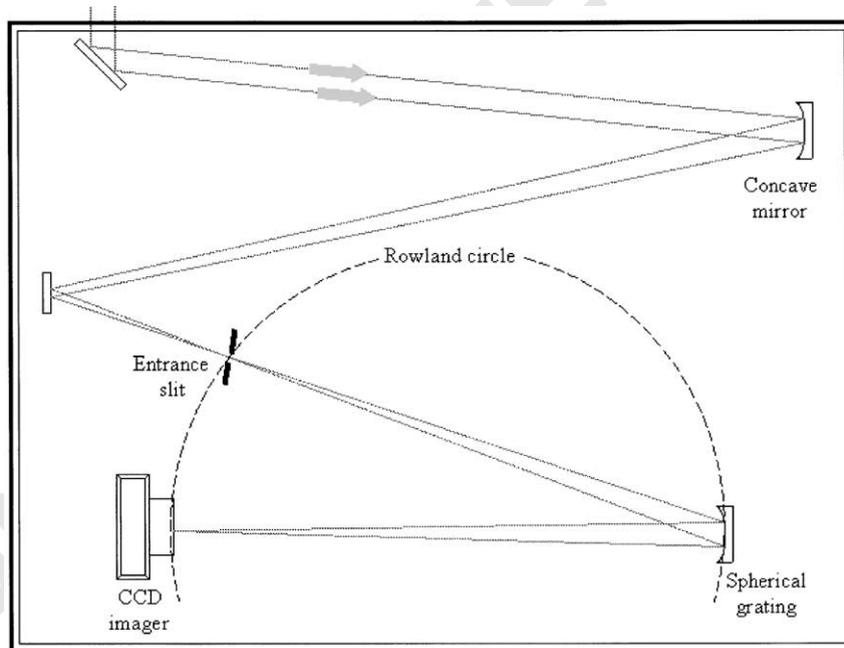


Fig. 1. A top view of the Paschen–Runge-type spectrometer for the analysis of the SASE FEL light.

Table 1	
Main parameters of the high-resolution spectrometer	
Grating	
Grooves/mm	600
Curvature radius (mm)	1000
Blaze wavelength (nm)	482
CCD camera	
Number of pixels	1100 × 330
Pixel size (μm)	24
Concave mirror curvature radius (mm)	4000
Spectral resolution (Å)	0.4
Bandpass (nm)	44
Resolving power at 530 nm	10000
Wavelength range (nm)	250–1100

3. Spectrum measurements

A typical spectrum of the spontaneous undulator radiation measured after the second section of the undulator is shown in Fig. 2. In order to explain the spectrum, let us consider the microscopic picture of the electron beam current at the entrance into the undulator. The electron beam current consists of electrons arriving at the entrance of the undulator at some particular time t_k :

$$I(t) = -e \sum_{k=1}^N \delta(t - t_k)$$

where N is the number of electrons in a bunch. The Fourier transform of the current can be written as

$$\bar{I}(\omega) = \int_{-\infty}^{\infty} e^{i\omega t} I(t) dt = -e \sum_{k=1}^N e^{i\omega t_k}$$

and the Fourier transform of the electric field emitted in the undulator can be expressed by

$$E(\omega) = e(\omega) \sum_k e^{i\omega t_k}$$

where $e(\omega)$ is the Fourier transform of an individual particle traveling through the undulator and is proportional to $\sin(\omega - \omega_0)T/(\omega - \omega_0)T$. The summation of a large number of exponentials with different arguments results in an appearance of sharp spikes in the $E(\omega)$ dependence, which can be seen in Fig. 2. The spike width is proportional to the reciprocal of the electron bunch length [6, 7].

The typical single shot spectra of the SASE light measured at different locations along the undulator line are presented in Fig. 3 (left column). The typical spectra simulated with the FEL code GINGER [8] for the same locations are shown in the right column.

3.1. Spectrum bandwidth

From the 1D theory of SASE, we know that in the exponential gain regime the spectrum width of the SASE light is given by [9]

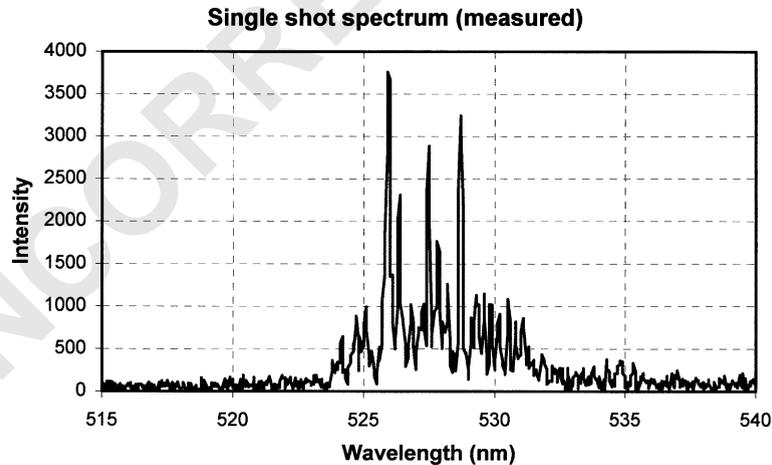


Fig. 2. Measured spectrum of spontaneous undulator radiation. FWHM bunch length is about 4 ps.

Single shot spectra

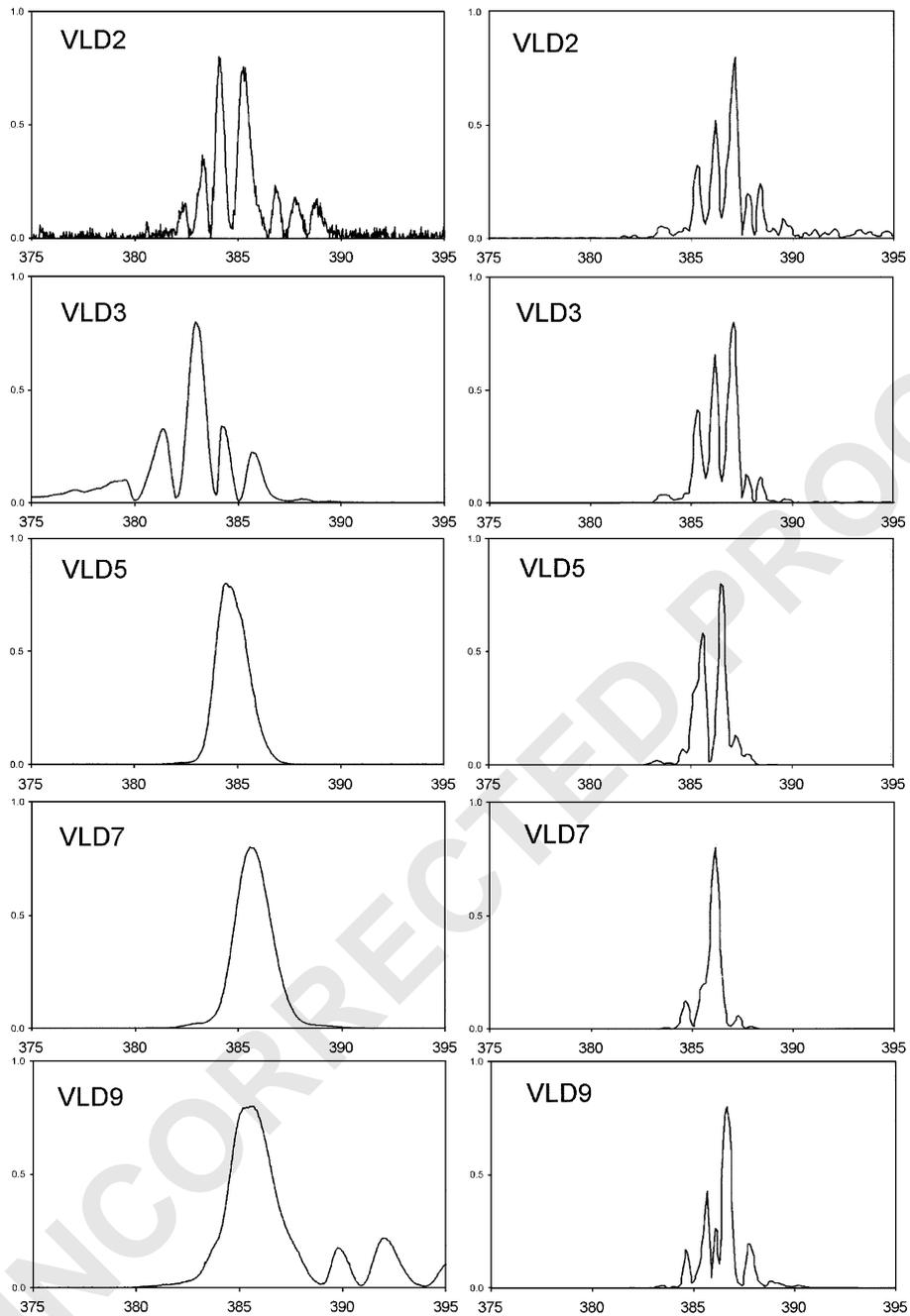


Fig. 3. Z-dependent single-shot spectrum measurements of the SASE radiation (left column) and simulations (right column). The saturation is achieved around undulator 7 (VLD 7).

$$\frac{\delta\lambda}{\lambda} = \sqrt{\frac{0.83\rho}{N_U}} \sim \frac{1}{\sqrt{z}}$$

where N_U is the number of undulator poles, ρ is the FEL scaling parameter, and z is the distance along the undulator.

Fig. 4 demonstrates the z -dependent rms spectrum width for both measurements and simulations. The simulations were done with the beam parameters shown in Ref. [5], Table 1, case C. The spectrum width does decrease along the undulator line until saturation is reached after undulator number 7. After saturation, the spectrum width increases again due to the synchrotron instability of the electrons and sideband development.

The measured and simulated curves of Fig. 4 show very similar z -dependent behavior. However, the absolute value of the measured spectrum width is about a factor of 1.6 larger. The reason for the difference in the measured and simulated spectral width is still not understood.

3.2. Spike width

For spontaneous radiation the width of the spectral spikes corresponds to the reciprocal of the bunch length. Because the electron bunches profile is not flat (usually somewhat Gaussian) and because the gain depends on the local electron bunch current, radiation emitted by different parts of the beam experiences different gain. One can view it as a decrease in the effective bunch length, since the radiation intensity in the central part of the Gaussian beam grows faster than in the rest of the beam. Therefore, the spike width will increase during the exponential gain regime. At saturation, other parts of the beam with lower local beam current will also come to saturation. This will result in an increase in the effective bunch length and a decrease in the spike width.

The spike width can be extracted from an autocorrelation of the spectrum. Fig. 5 shows the autocorrelation averaged over many shots for several VLD stations for simulated and measured spectra. The z -dependence of the spike width obtained with the autocorrelation is plotted in Fig. 6. As expected, the spike width increases in

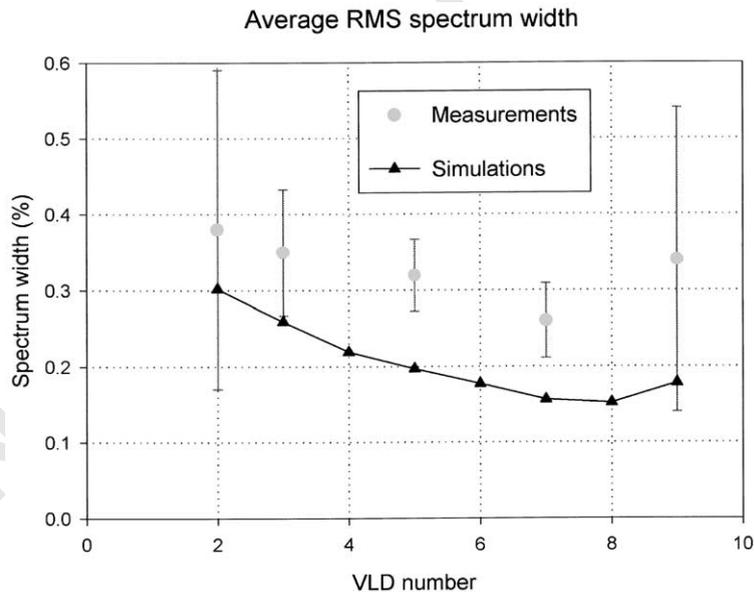
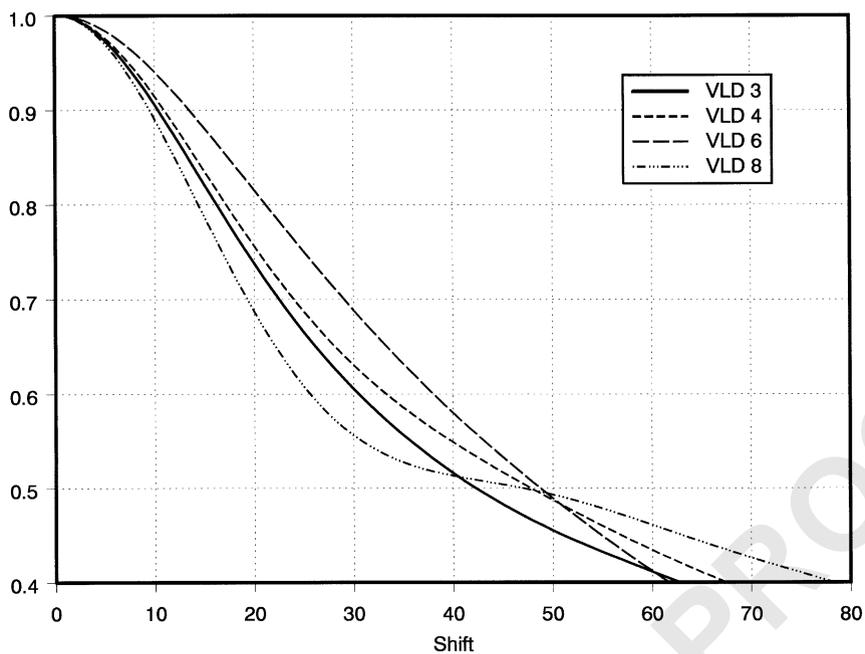


Fig. 4. RMS spectrum width for measurements and simulations. Error bars show standard deviation of the width fluctuations.

Spectrum autocorrelation (measured)



Spectrum autocorrelation (simulations)

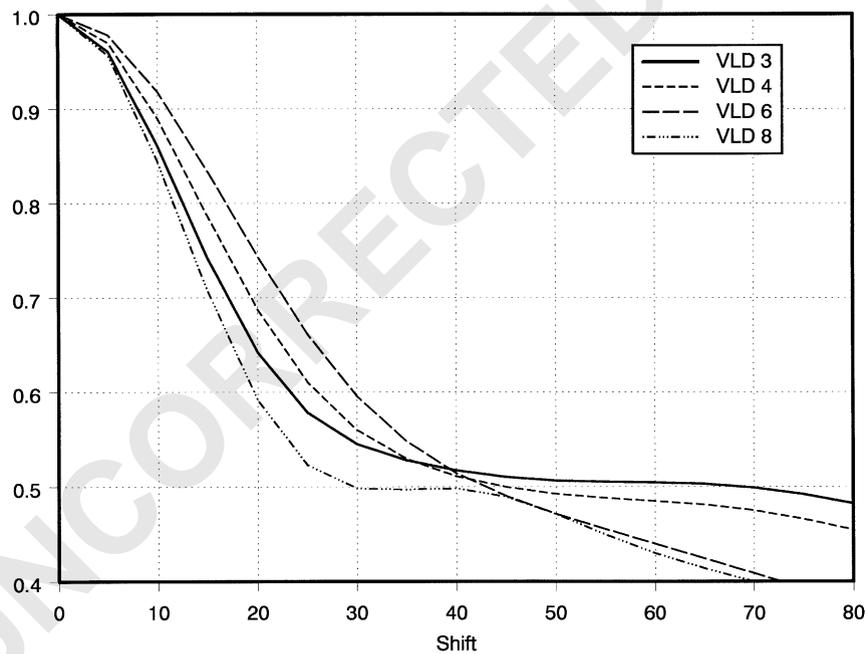


Fig. 5. Average spectrum autocorrelation for measured (top) and simulated (bottom) spectra.

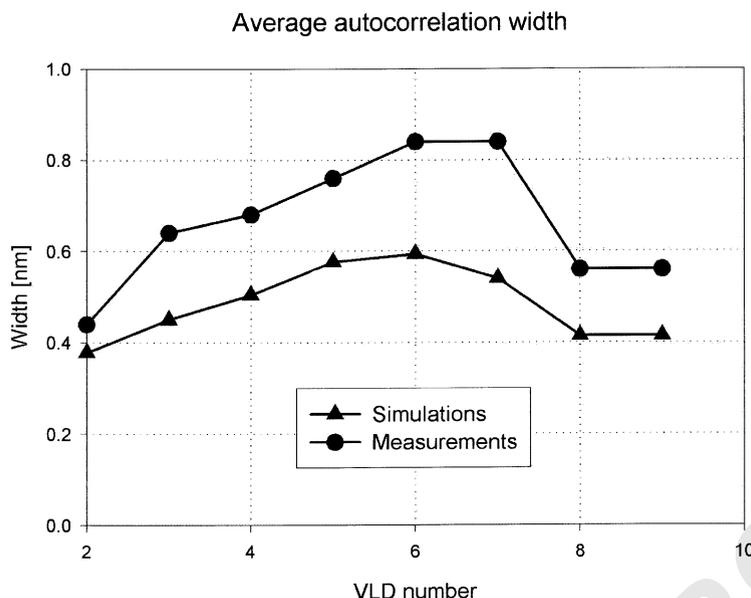


Fig. 6. Average spike width along the undulator line for measured and simulated spectra.

the exponential gain regime up to saturation, and then it decreases due to new sidebands appearing after the saturation. The measured and calculated spike widths of Fig. 6 show similar behavior along the undulator line; however, the absolute spike width of the measured spectra is about a factor of 1.5 larger. The fact that the measured spikes are wider than the simulated ones can also be noticed in Fig. 3.

The difference in the spike width can be explained in several ways. First, the estimated accuracy of the electron bunch length measurements is about 20% rms. This could give an error close to a factor of 1.5. Second, the bunch profile could contain an intense core that is shorter than the overall bunch but provides most of the radiation. Finally, it could be a combination of the reasons mentioned above.

3.3. Average number of spikes

As one can see from Fig. 3, the number of spikes in the spectrum also decreases with the distance along the undulator. The number of spectral spikes corresponds to the number of coherence

modes. Since the coherence length increases along the undulator, the number of coherent modes decreases, resulting in a decreased number of spikes. When saturation is achieved, the sidebands appear, increasing the number of spikes again as one can see from the last row in Fig. 3. An average number of spikes in the spectrum calculated for different locations along the undulator line is presented in Fig. 7.

4. Vertical angle dependence of the wavelength

Due to astigmatism of the spherical grating in the spectrometer, the horizontal and vertical focuses of the spectral image are not achieved simultaneously. That is why the image on the CCD camera has non-zero vertical size, and the vertical direction corresponds to the vertical angle in the SASE light.

Fig. 8 shows one of the images recorded by the CCD camera. The horizontal direction on the image corresponds to the wavelength of the radiation while the vertical direction corresponds to the vertical angle of the radiation. Analysis of

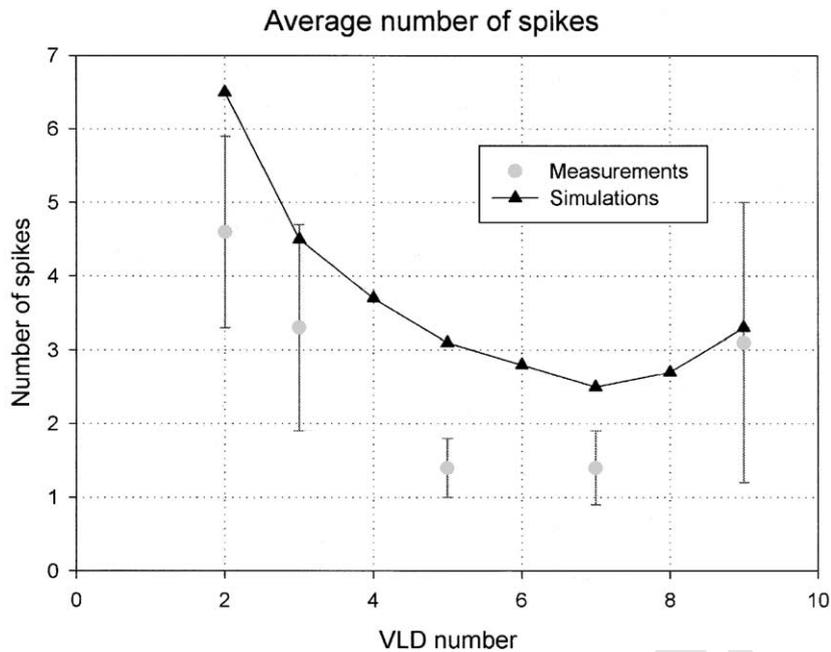


Fig. 7. Average number of spikes in the spectrum at different locations along the undulator. Error bars show standard deviation of the number of spikes fluctuations.

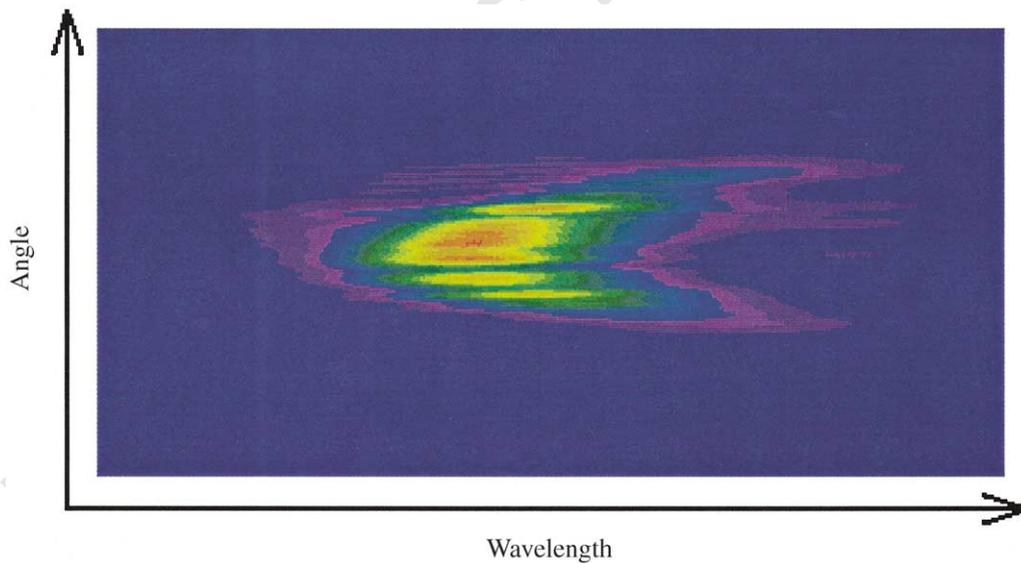


Fig. 8. Spectral image of the radiation after VLD 4. Horizontal direction is wavelength; vertical direction is vertical angle of radiation.

such images allows one to extract the vertical angle dependence of the radiated wavelength of the SASE light.

During the exponential growth of SASE light, a single transverse mode dominates over all other modes at a given radiation wavelength within the gain bandwidth. However, the mode characteristics at one wavelength are different from that of the other wavelength [10]. More specifically, the angular divergence of the transverse mode increases somewhat with the increasing wavelength due to stronger diffraction. As a result, the central wavelength observed at an angle θ with respect to the z -axis is slightly red-shifted. Fig. 9 shows the measured central wavelength as a function of the vertical angle, obtained from the image shown above. Calculations based on the 3D FEL mode theory show close agreement (solid curve). For comparison, the angular dependence of the radiation wavelength for spontaneous emission is given by

$$\frac{\delta\lambda}{\lambda} = \frac{\gamma^2\theta^2}{1 + K^2/2}$$

where γ is the relativistic factor of the electron

beam and K is the undulator parameter. It is also plotted in Fig. 9 (dash curve). As expected, the angular dependence is much stronger for spontaneous emission than for SASE.

The curvature of the spectral image can slightly increase measured spectrum width and spike width. The image processing software extracts a curve by integrating over some vertical intervals of the image, so the resulting spectrum can be wider than the original one. Accurate comparisons of spectral images with their integrated projections show that a spectrum width increase of up to 20% is possible, when the vertical integration intervals are not optimally chosen.

The spectral images can also be used for determining the angular distribution of the radiation intensity. Fig. 10 shows the intensity plot obtained from the image above. This plot gives rms angular divergence of the SASE radiation of 0.5 mrad, which is in good agreement with the values obtained from other measurements.

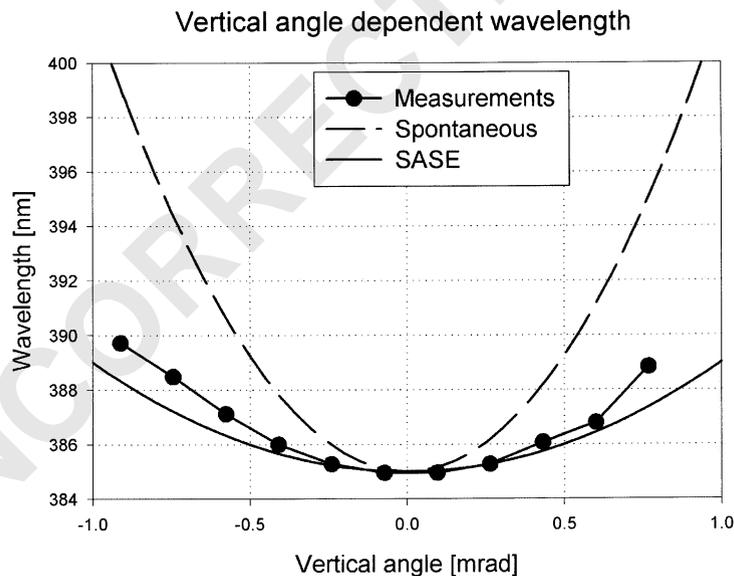


Fig. 9. Wavelength dependence on the vertical radiation angle. Dash and solid lines are expected curve for the spontaneous emission and for SASE radiation; circles are measurements.

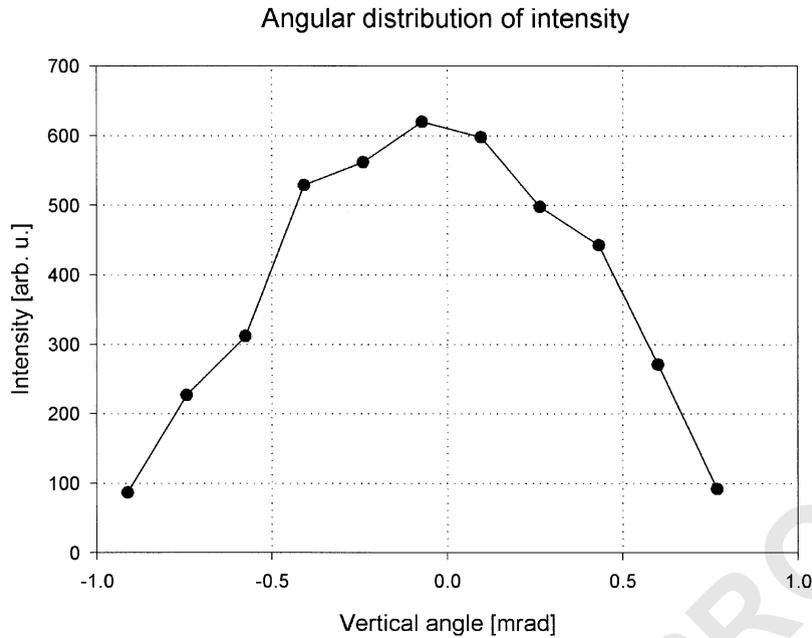


Fig. 10. Angular distribution of the SASE radiation intensity.

2nd harmonic λ 1st harmonic λ

Fig. 11. Spectral image showing simultaneously first and second harmonics of the SASE radiation. Top left part of the image is the second harmonic spectrum; bottom right is the first harmonic spectrum. Wavelength direction is reversed for the first harmonic image because one more mirror was used to direct the first harmonic image onto the CCD camera.

5. Second harmonic measurements

The non-linear harmonics of the fundamental wavelength are expected to grow after the bunch-

ing at the fundamental is apparent [11,12]. In the case of a planar undulator, the odd harmonics are favored due to the natural sinusoidal motion of the electron beam in the undulator, although the

second harmonics is fairly significant, too. From the simulations [11], one can expect about a factor of 10^3 power reduction of the second harmonic compared to the fundamental.

Minor modification of the spectrometer configuration allows measurement of the spectrum of the first and second harmonics of the SASE radiation simultaneously. The CCD camera is placed at the

location of the spectral image of the second harmonic, and one additional mirror at the center of the Rowland circle is used to direct the image of the first harmonic onto the CCD. Fig. 11 shows a typical spectral image with two spectra: the upper one is the second harmonic spectrum and the lower one is the fundamental harmonic. The first harmonic was attenuated by a factor of 10^3 .

Simultaneous single shot spectra of 1st and 2nd harmonics

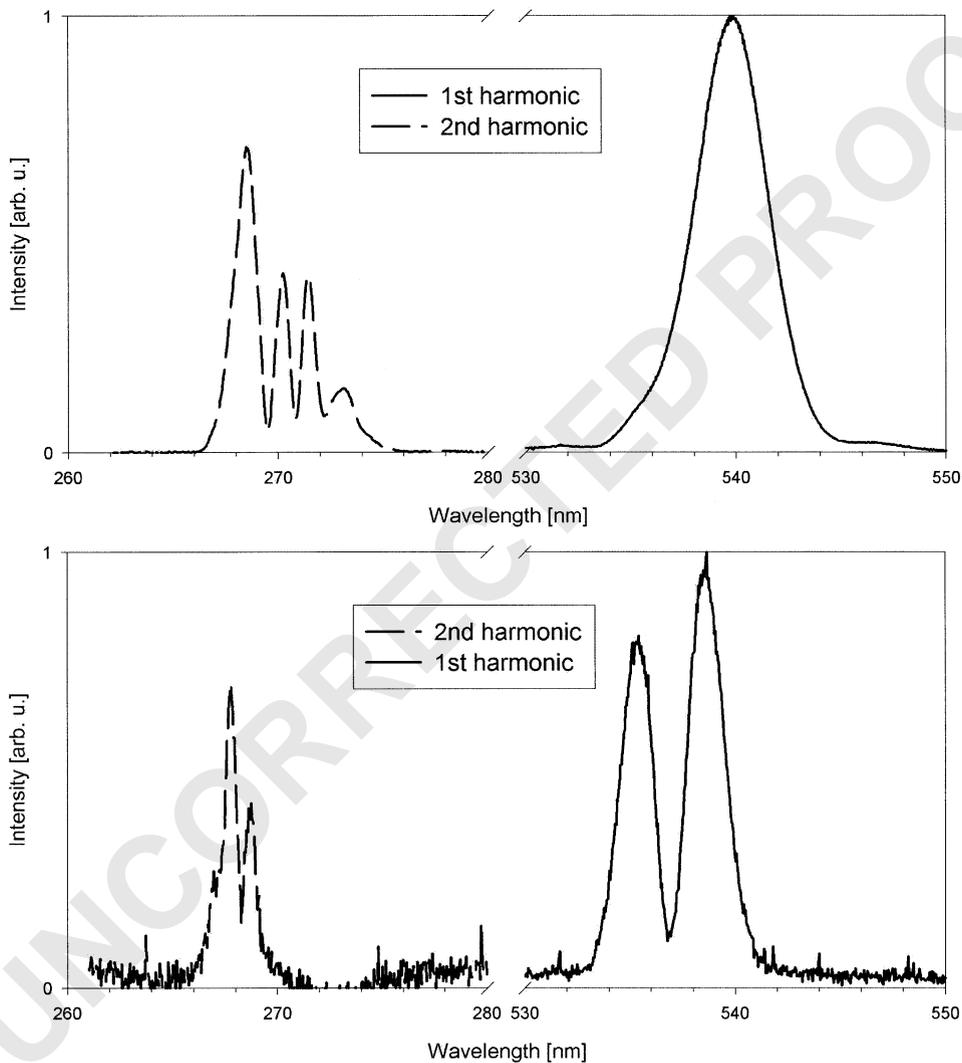


Fig. 12. Spectral plots showing simultaneous measurements of the first (solid curve) and second (dash curve) harmonics for two different shots.

Fig. 12 shows two typical plots showing the first and second harmonic spectra. These two plots were chosen to demonstrate that the spectral shape of the two harmonics could be different (left) or similar (right). The average rms spectrum width of the two harmonics has been calculated for the SASE radiation after the undulator

$$1st\ harmonic\ (530\ nm)\ \frac{\delta\lambda}{\lambda} = 2.9 \times 10^{-3}$$

$$2nd\ harmonic\ (265\ nm)\ \frac{\delta\lambda}{\lambda} = 4.4 \times 10^{-3}.$$

6. Conclusions

The z -dependence of the spectrum of SASE FEL radiation has been measured. It shows a narrowing of the spectral bandwidth during the exponential gain regime and the appearance of sidebands after saturation is achieved. Qualitative behavior of the measured spectra coincides very well with the theory and simulations. However, there are still some quantitative differences that could be attributed to both measurements processing difficulties and simulation complexity. It is hoped that these data will further stimulate SASE modeling devel-

opment for the fundamental and higher harmonics.

References

- [1] S.V. Milton, et al., Nucl. Instr. and Meth. A 407 (1998) 210. 29
- [2] S.V. Milton, et al., Proc. SPIE 3614 (1999) 96. 31
- [3] I.B. Vasserman, et al., Proceedings of the PAC 1999, p. 2489. 33
- [4] E. Gluskin, et al., Nucl. Instr. and Meth. A 429 (1999) 358. 35
- [5] S. Milton, et al., Science 292 (2001) 2037. Originally published in Science Express as 10.1126/science.1059955 on May 17, 2001. 37
- [6] M. Zolotarev, G. Stupakov, SLAC-PUB-7132, March 1996. 39
- [7] E. Saldin, E. Schneidmiller, M. Yurkov, Statistical properties of radiation from VUV and X-ray FEL, DESY preprint TESLA-FEL97-02, April 1997. 41
- [8] W. Fawley, An informal manual for GINGER and its post-processor XPLOTGIN, BP Technical Note-104, LBNL, Berkeley, CA, 1995. 43
- [9] K.-J. Kim, Nucl. Instr. and Meth. A 250 (1986) 396. 45
- [10] K.-J. Kim, Z. Huang, Present Status of X-ray FELs, AIP Conference Proceedings 581, Physics of and Science with the X-ray Free-Electron Laser, 2001, p. 185. 47
- [11] H.P. Freund, S.G. Biedron, S.V. Milton, IEEE J. Quant. Electron. 36 (2000) 275 and references therein. 49
- [12] Z. Huang, K.-J. Kim, Phys. Rev. 62E (2000) 7295 and references therein. 51

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